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Math 1571

**I. Find  $\frac{dy}{dx}$  for each of the following:**

1.  $y = \sqrt{x^3 \tan(x^4)}$
2.  $y = \cos(\tan(x))$
3.  $x \sin(y) = y - 1$
4.  $y\sqrt{(x-1)} + x\sqrt{(y-1)} = xy$
5.  $y = \frac{(x-1)(x-4)}{(x-2)}$
6.  $y = \frac{\sin(2x)}{x}$

**II. Find  $\frac{dy}{dx}$  for each of the following:**

1. If  $y = \frac{1}{\sqrt{4x-3x^2}}$
2.  $y = 3x + \cos(x)$
3.  $y = \frac{x^3}{4 - \sin(2x)}$
4.  $y = [5x^2 + \cos(2x)]^3$
5.  $y = \sin(x) \cos(2x)$
6.  $y = \tan^4(5x^2 - 3x)$
7.  $yx - y^2 = 6$

**III. Simplify Find  $y''$  by implicit differentiation and simplify.**

1.  $x^2 - y^2 = 1$
2. If  $y = 2 \cos(x) + \sin^2(x)$  find  $y', y''$
3. If  $f'(x) = \frac{x}{(x+2)(x+3)}$ , where is  $f$  increasing/decreasing. (*Note :  $f'$  is given*)
4. If  $f''(x) = \frac{5x}{x+1}$  then where is  $f$  concave upward/downward. (*Note :  $f''$  is given*)

**IV. Find for  $f(x)$**

- a. The Domain,
- b. The Intercepts,
- c. Symmetry,
- d. Asymptotes (horizontal and vertical),
- e. Intervals of increasing/decreasing,
- f. Max/min,
- g. Concave up/down,
- h. Points of inflection and
- g. Sketch.

where the function is:

1.  $y = x^4 - 2x^2$
2.  $y = \frac{x^2 - 1}{x}$

3.  $y = \frac{x^2 + 1}{(x^2 - 4)}$
4.  $y = \cos(x) + \sin(x)$  on the interval  $[0, 4\pi]$ .
5.  $y = \frac{(x)}{2} - \sin(x)$  on the interval  $[0, 3\pi]$ .
6. If  $f(x) = \frac{x}{(x + 2)(x + 3)}$ ,
7. If  $f(x) = \frac{5x}{x + 1}$
8.  $y = \frac{1}{3}x^3 - \frac{1}{2}x^2 + 1$
9.  $y = \frac{2}{3}x^3 - x^2 - 4x + 2$
10.  $y = x^4 - 2x^2$